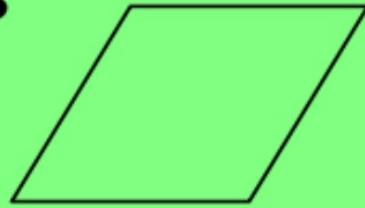


## 6-4: Special Parallelograms

### **RHOMBUS**



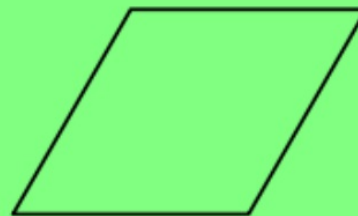
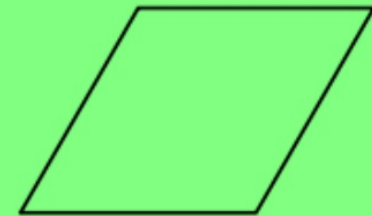
**A parallelogram with**

\_\_\_\_\_.

### Theorems:

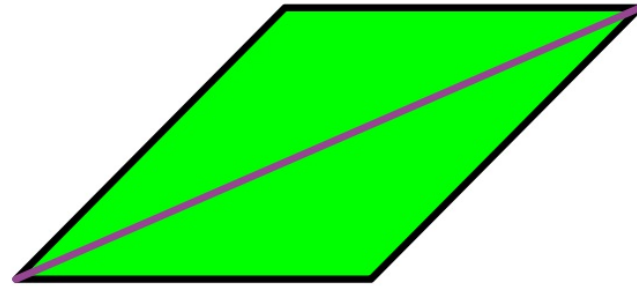
1. Each diagonal of a rhombus bisects two angles of the rhombus.

2. The diagonals of a rhombus are perpendicular.

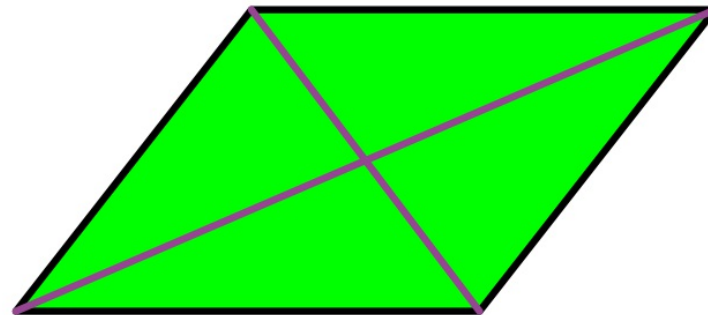


## More Theorems

3. If one diagonal of a parallelogram bisects two angles of the parallelogram, then the parallelogram is a rhombus.



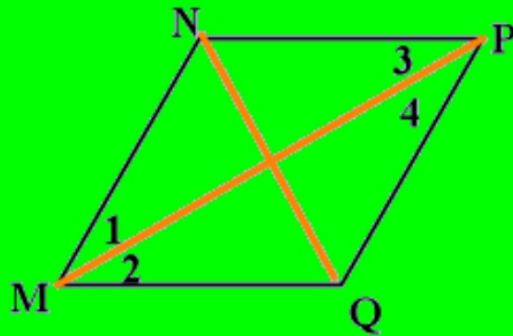
4. If the diagonals of a parallelogram are perpendicular, then the parallelogram is a rhombus.



*Each diagonal of a rhombus bisects two angles of the rhombus.  
The diagonals of a rhombus are perpendicular.*

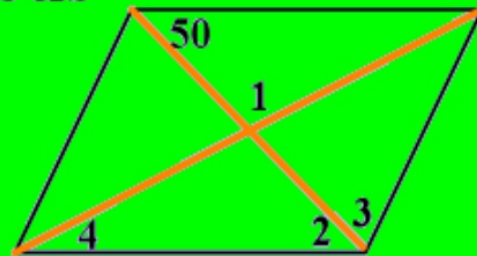
### **Examples:**

**1) MNPQ is a rhombus and  $m\angle N = 120^\circ$ . Find the measures of the numbered angles.**



*Each diagonal of a rhombus bisects two angles of the rhombus.  
The diagonals of a rhombus are perpendicular.*

**2) Find the measures of the numbered angles in the rhombus**



# Rectangles



A rectangle is a parallelogram with \_\_\_\_\_.

## Theorems:

1. The diagonals of a rectangle are congruent.



2. If the diagonals of a parallelogram are congruent, then the parallelogram is a rectangle.



*The diagonals of a rectangle are congruent.*

*If the diagonals of a parallelogram are congruent, then the parallelogram is a rectangle.*

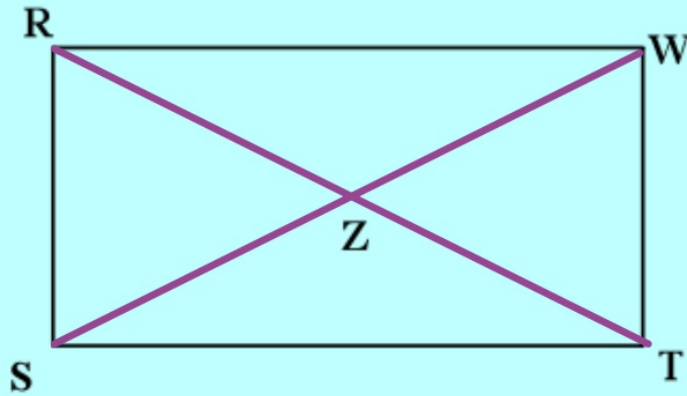
**Examples:**

**1. ABCD is a rectangle. Find the value of  $x$  and the length of each diagonal if  $AC = 5x - 9$  and  $BD = x + 5$ .**

*The diagonals of a rectangle are congruent.*

*If the diagonals of a parallelogram are congruent, then the parallelogram is a rectangle.*

2.



$$\mathbf{RZ = 2x + 5}$$

$$\mathbf{SW = 5x - 20}$$

*The diagonals of a rectangle are congruent.*

*If the diagonals of a parallelogram are congruent, then the parallelogram is a rectangle.*

**2. Can you conclude that the parallelogram is a rhombus or rectangle? Explain.**

**a. The diagonals of ABCD are perpendicular.  
AB = 16cm and BC = 8cm.**

**b. A parallelogram has angles of 30, 150, 30  
and 150 degrees.**